

### References

- <sup>1</sup>Anon., "All Weather Carrier Landing System Airborne Subsystem, General Requirements for," AR-40, May 1969, Naval Air Systems Command, Washington, D. C.
- <sup>2</sup>Durand, T.J., "Carrier Landing Analyses," Rept 137-2, Feb. 1967, Systems Technology, Inc., Hawthorne, Calif.
- <sup>3</sup>Anon., "Proposal for a SPN-42 DMC Lead Computer," Tech. Proposal No. 251, May 1972, Systems Technology, Inc., Hawthorne, Calif.
- <sup>4</sup>Christie, W.B. and Shust, A.P., "Development of the A-7E Airplane Automatic Carrier Landing System (ACLS) Mode I Operational Capability," Rept. FT-28R-72, May 1972, Naval Air Test Center, Warminster, Pa.
- <sup>5</sup>Craig, S.J., Ringland, R.F. and Ashkenas, I.L., "An Analysis of Navy Approach Power Compensator Problems and Requirements," Rept. 197-1, March 1971, Systems Technology, Inc. Hawthorne, Calif.
- <sup>6</sup>Durand, T.S. and Teper, G.L., "An Analysis of Terminal Flight Path Control in Carrier Landings," Rept. 137-1, Aug 1964, Systems Technology, Inc., Hawthorne, Calif.
- <sup>7</sup>Judd, T.M., "A Modified Design Concept Utilizing Deck Motion Prediction, for the A-7E Automatic Carrier Landing System," MS thesis, June 1973, Dept. of Aeronautics, Naval Postgraduate School, Monterey, Calif.

## Representation of the Drag Polar of a Fighter Aircraft

Kirit S. Yajnik\* and Malladi V. Subbaiah†

National Aeronautical Laboratory, Bangalore, India

### Introduction

THE possibility of an analytical approximation of the drag polar of a fighter aircraft which would be applicable to the large values of angles of attack encountered in maneuvers is considered. Evidently, a simple representation can be conveniently used for making rather accurate estimates of turn performance in aircraft design and evaluation, and in the optimization of flight paths.

The classical representation, which approximates the drag coefficient,  $C_D$ , by  $C_{D0} + kC_L^2$ , is compared in Fig. 1 with the drag polars of YF-16.<sup>1</sup> In order to ensure the accuracy of the classical representation near zero  $C_L$ , the drag coefficient at zero  $C_L$ ,  $C_{D0}$ , and the induced drag coefficient  $k$  are chosen so that the classical curve is tangent to the curve of the square of the lift coefficient,  $C_L$ , vs  $C_D$ . The need for an improved representation is evident. It is also clear that strakes and automatically controlled flaps do not change the qualitative nature of the curve. Available data on other fighter configurations further suggests that the nonlinearity indicated in Fig. 1 is quite typical.

The slope of the  $C_L^2$  vs  $C_D$  curve changes gradually rather than abruptly, which is probably due to the gradual spanwise spread of the separated regions on the wing with increasing angle of attack. It is therefore inappropriate to approximate the curve by two straight lines. What is called for is an additive correction  $f(C_L)$  to the classical representation that is insignificant at small values of  $C_L^2$ . This Note investigates simple functional forms of  $f$  that are capable of describing the available drag polars.

Received October 14, 1975; revision received December 22, 1975.

Index categories: Aircraft Aerodynamics (including Component Aerodynamics); Aircraft Performance.

\*Scientist, Aerodynamics Division.

†Scientist, Aerodynamics Division. Presently at California Institute of Technology.

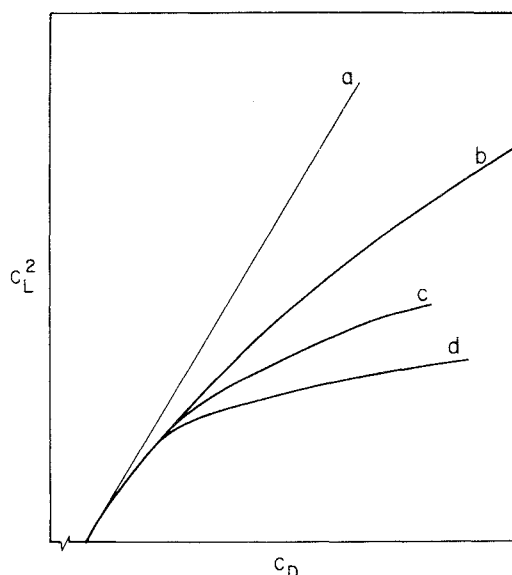


Fig. 1 The classical approximation (a) and the drag polars of YF-16 configurations.<sup>1</sup> (b) with variable LE flap and strake; (c) with flap only; (d) without flap or strake.

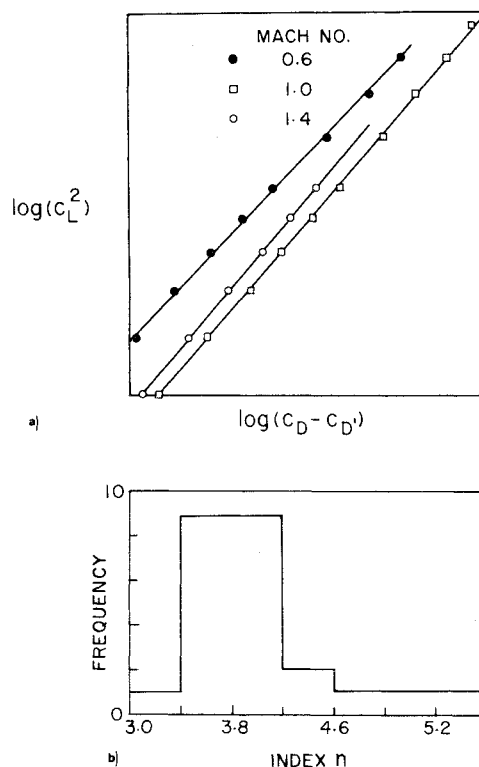


Fig. 2 The nature of the additive correction: a)  $C - C_D' - aC_L^n$ ; b) the histogram of  $n$  for a sample of 24 drag polars.

### Method and Results

A first step in examining the forms of the correction was to determine the appropriate classical approximation for the given drag polar. Since much of the data was available in the graphical form, a graphical method was chosen. A tangent was drawn to the smoothed  $C_L^2$  vs  $C_D$  curve at the minimum  $C_D$  point, where the value of  $C_L$  was usually negligible. Let  $C_D$  and  $C_D'$  refer to the values on the given drag polar and on the tangent at a given value of  $C_L$ .  $(C_D - C_D')$  then gives the required correction. It was plotted against  $C_L^2$  on a log-log plot. Figure 2 gives typical cases and shows that a straight line

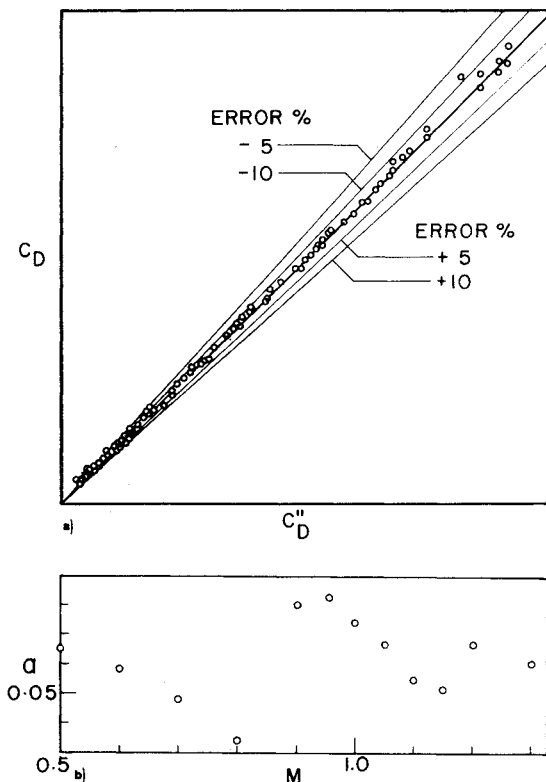


Fig. 3 a) Effectiveness of the representation given by Eq. (2); b) variation of  $a$  with Mach number,  $M$ .

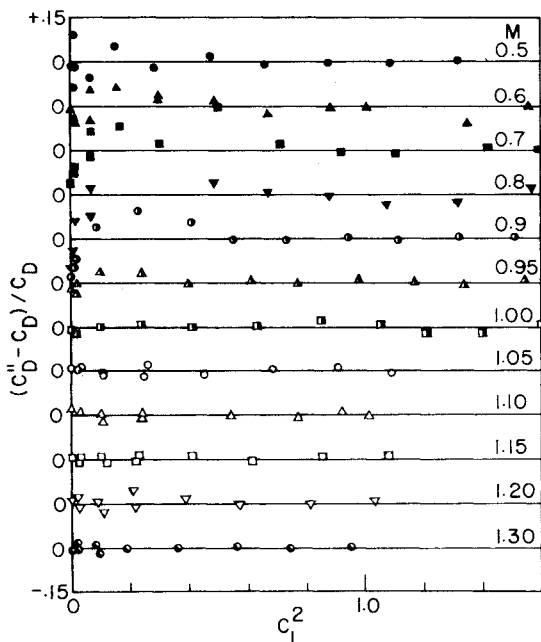


Fig. 4 The distribution of relative error  $(C_D'' - C_D)/C_D$  in subsonic, transonic and supersonic range.

can well approximate the curve. Hence it is reasonable to take the correction as

$$f = (C_D - C_D') = aC_L^n \quad (1)$$

where the coefficients  $a$  and  $n$  have to be chosen for the given drag polar. The histogram of  $n$  (Fig. 2) shows that the three-fourth of the sample under study has  $n$  ranging from 3.4 to 4.2.

Further examination showed that the values of  $n$  were sensitive to the details of the method of determining  $C_D'$ . For instance, if a line with a slightly different slope was judged as a tangent, the value of  $f$  could significantly change for large  $C_L$ . A numerical method was selected to reduce the uncertainties. The classical representation was first fitted as a line of regression of  $C_D$  on  $C_L^2$  to the four experimental data points having the smallest values of  $C_L^2$ . The index  $n$  was then found from the line of regression of  $\log(C_D - C_D')$  on  $\log(C_L^2)$ . The values showed an increase in the transonic range. Also, differences between the numerically and the graphically obtained values of  $n$  were often significant.

Since  $n$  seemed to be rather sensitive to extraneous details, it was felt that a simpler representation, if sufficiently accurate, is to be preferred. With this view, we examined the simpler representation

$$C_D'' = C_{D0} + kC_L^2 + aC_L^4 \quad (2)$$

The above expression can be considered as a quadratic curve of regression of  $C_D$  on  $C_L^2$ . The examination was restricted to two configurations for which we had detailed data.

The calculated values  $C_D''$  are compared with the experimental values of  $C_D$  in Fig. 3. There is no evidence of a systematic departure. Also, the index of correlation of Eq. (2), which is the ratio of standard deviations of  $C_D''$  and  $C_D$ , was typically in the range of 0.997 to 0.999. The closeness of this index to 1 is an indication of the effectiveness of the representation equation (2).

Figure 4 shows the relative error in the subsonic, the transonic, and the supersonic range. Evidently, the agreement of  $C_D''$  with the experimental values is better than 3% in the transonic and the supersonic range, perhaps due to the reduced relative error in measuring larger forces and the smaller range of  $C_L$ . While the relative errors are somewhat larger in the subsonic range, the agreement is still fairly satisfactory.

### Conclusion

The present study suggests that the simple analytical approximation (2) can be advantageously used in the turn calculations of a fighter aircraft. The magnitude of  $a$  is of the order of  $k$  and hence  $aC_L^4$  is comparable to  $kC_L^2$  when  $C_L$  is of the order of unity. The variation of  $a$  with Mach number is shown in Fig. 3.

### Reference

1. Buckner, J. K., Hill, P. W., and Benope, D., "Aerodynamic Design Evaluation of the YF-16", AIAA Paper 74-935, Los Angeles, Calif., 1974.

## Engine Life Cycle Cost: A Laboratory View

Robert F. Panella\*

Air Force Aero Propulsion Laboratory,  
Wright-Patterson AFB, Ohio

**L**IFE cycle cost (LCC) is defined by Air Force Regulation 800-11 as "the total cost of an item or system over its full life." As applied to airbreathing engines, it includes the cost to develop and test the engine during the engineering development phase; the cost to produce the engine in quantity during

Presented as Paper 75-1287 at the AIAA/ASME 11th Propulsion Conference, Anaheim, Calif., September 29-October 1, 1975; submitted October 20, 1975; revision received December 8, 1975.

Index category: Aircraft Economics.

\*Project Manager, APSI Program.